

**MARK SCHEME for the May/June 2014 series**

**4037 ADDITIONAL MATHEMATICS**

**4037/11**

Paper 1, maximum raw mark 80

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

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<p><b>1</b></p> $\text{LHS} = \frac{\sin \theta}{\cos \theta} + \frac{\cos \theta}{1 + \sin \theta}$ $= \frac{\sin \theta(1 + \sin \theta) + \cos^2 \theta}{\cos \theta(1 + \sin \theta)}$ $= \frac{1 + \sin \theta}{\cos \theta(1 + \sin \theta)}$ $= \frac{1}{\cos \theta} \text{ leading to } \sec \theta$ <p><b>Alternative solution:</b></p> $\text{LHS} = \frac{\sin \theta}{\cos \theta} + \frac{\cos \theta(1 - \sin \theta)}{(1 + \sin \theta)(1 - \sin \theta)}$ $= \frac{\sin \theta}{\cos \theta} + \frac{\cos \theta(1 - \sin \theta)}{\cos^2 \theta}$ $= \frac{\sin \theta}{\cos \theta} + \frac{(1 - \sin \theta)}{\cos \theta}$ $= \frac{1}{\cos \theta} \text{ leading to } \sec \theta$ <p><b>Alternative solution:</b></p> $\text{LHS} = \frac{\tan \theta(1 + \sin \theta) + \cos \theta}{1 + \sin \theta}$ $= \frac{\frac{\sin \theta}{\cos \theta} + \frac{\sin^2}{\cos \theta} + \cos \theta}{1 + \sin \theta}$ $= \frac{\sin \theta + \sin^2 \theta + \cos^2 \theta}{\cos \theta(1 + \sin \theta)}$ $= \frac{1 + \sin \theta}{\cos \theta(1 + \sin \theta)}$ $= \frac{1}{\cos \theta} \text{ leading to } \sec \theta$	<p><b>B1</b></p> <p><b>M1</b></p> <p><b>DM1</b></p> <p><b>A1</b></p> <p><b>B1</b></p> <p><b>M1</b></p> <p><b>DM1</b></p> <p><b>A1</b></p> <p><b>M1</b></p> <p><b>B1</b></p> <p><b>DM1</b></p> <p><b>A1</b></p>	<p><b>B1</b> for use of <math>\tan \theta = \frac{\sin \theta}{\cos \theta}</math></p> <p><b>M1</b> for attempt to obtain a single fraction</p> <p><b>DM1</b> for use of <math>\sin^2 \theta + \cos^2 \theta = 1</math></p> <p><b>A1</b> for ‘finishing off’</p> <p><b>B1</b> for use of <math>\tan \theta = \frac{\sin \theta}{\cos \theta}</math></p> <p><b>M1</b> for multiplication by <math>(1 - \sin \theta)</math></p> <p><b>DM1</b> for use of <math>\sin^2 \theta + \cos^2 \theta = 1</math></p> <p><b>A1</b> for ‘finishing off’</p> <p><b>M1</b> for attempt to obtain a single fraction</p> <p><b>B1</b> for use of <math>\tan \theta = \frac{\sin \theta}{\cos \theta}</math></p> <p><b>DM1</b> for use of <math>\sin^2 \theta + \cos^2 \theta = 1</math></p> <p><b>A1</b> for ‘finishing off’</p>
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<p>6 (i)</p> $\mathbf{AB} = \begin{pmatrix} 10 & 19 \\ 32 & 37 \\ 14 & 14 \end{pmatrix}$ <p>(ii)</p> $\mathbf{B}^{-1} = \frac{1}{7} \begin{pmatrix} 5 & -1 \\ -3 & 2 \end{pmatrix}$ <p>(iii)</p> $2 \begin{pmatrix} 2 & 1 \\ 3 & 5 \end{pmatrix} \begin{pmatrix} x \\ y \end{pmatrix} = \begin{pmatrix} -3 \\ -22 \end{pmatrix}$ $\begin{pmatrix} x \\ y \end{pmatrix} = \frac{1}{7} \begin{pmatrix} 5 & -1 \\ -3 & 2 \end{pmatrix} \begin{pmatrix} -1.5 \\ -11 \end{pmatrix} = \frac{1}{7} \begin{pmatrix} 3.5 \\ -17.5 \end{pmatrix}$ <p><math>x = 0.5, y = -2.5</math></p>	<p>M1</p> <p>A1</p> <p>B1</p> <p>B1</p> <p>M1</p> <p>M1</p> <p>A1</p>	<p>M1 for at least 3 correct elements of a <math>3 \times 2</math> matrix</p> <p>A1 for all correct</p> <p>B1 for <math>\frac{1}{7}</math>, B1 for <math>\begin{pmatrix} 5 &amp; -1 \\ -3 &amp; 2 \end{pmatrix}</math></p> <p>M1 for obtaining in matrix form</p> <p>M1 for pre-multiplying by <math>\mathbf{B}^{-1}</math></p> <p>A1 for both</p>
<p>7 (i)</p> $y = 2x^2 - \frac{1}{x+1} (+c)$ <p>when <math>x = \frac{1}{2}, y = \frac{5}{6}</math> so <math>\frac{5}{6} = \frac{1}{2} - \frac{2}{3} + c</math></p> <p>leading to <math>c = 1</math></p> $\left( y = 2x^2 - \frac{1}{x+1} + 1 \right)$ <p>(ii)</p> <p>When <math>x = 1, y = \frac{5}{2}</math></p> $\frac{dy}{dx} = \frac{17}{4} \text{ so gradient of normal} = -\frac{4}{17}$ <p>Equation of normal <math>y - \frac{5}{2} = -\frac{4}{17}(x - 1)</math></p> $(8x + 34y - 93 = 0)$	<p>B1</p> <p>B1</p> <p>M1</p> <p>A1</p> <p>M1</p> <p>B1</p> <p>DM1</p> <p>A1</p>	<p>B1 for each correct term</p> <p>M1 for attempt to find <math>+c</math>, must have at least 1 of the previous B marks</p> <p>Allow A1 for <math>c = 1</math></p> <p>M1 for using <math>x = 1</math> in their (i) to find <math>y</math></p> <p>B1 for gradient of normal</p> <p>DM1 for attempt at <b>normal</b> equation</p> <p>A1 – allow unsimplified (fractions must not contain decimals)</p>



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<b>10 (a)</b>	1 digit even numbers	2	<b>B1</b>		
	2 digit even numbers	$4 \times 2 = 8$	<b>B1</b>		
	3 digit even numbers	$3 \times 3 \times 2 = 18$	<b>B1</b>		
	Total = 28		<b>B1</b>		
	<b>(b) (i)</b>	3M 5W = 35		<b>B1</b>	
		4M 4W = 175		<b>B1</b>	
		5M 3W = 210		<b>B1</b>	
	Total = 420		<b>B1</b>	<b>B1</b> for addition to obtain final answer, must be evaluated.	
	<b>(ii)</b>	or ${}^{12}C_8 - 6M 2W - 7M 1W$			or: as above, final <b>B1</b> for subtraction to get final answer
		$495 - 70 - 5 = 420$			
	Oldest man in, oldest woman out and vice-versa				
	${}^{10}C_7 \times 2 = 240$		<b>B1, B1</b>	<b>B1</b> for ${}^{10}C_7$ , B1 for realising there are 2 identical cases	
	<b>Alternative:</b>				
	1 man out                      1 woman in				
	6 men                              4 women				
	6M 1W : ${}^6C_6 \times {}^4C_1 = 4$				
	5M 2W : ${}^6C_5 \times {}^4C_2 = 36$				
	4M 3W : ${}^6C_4 \times {}^4C_3 = 60$				
	3M 4W : ${}^6C_3 \times {}^4C_4 = 20$				
	Total = 120		<b>B1</b>	All separate cases correct for <b>B1</b>	
	There are 2 identical cases to consider, so 240 ways in all.		<b>B1</b>	<b>B1</b> for realising there are 2 identical cases, which have integer values	

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<p>11 (a)</p>	$5\sin 2x + 3\cos 2x = 0$ $\tan 2x = -0.6$ $2x = 149^\circ, 329^\circ$ $x = 74.5^\circ, 164.5^\circ$ <p><b>Alternatives:</b>  <math>\sin(2x + 31^\circ) = 0</math> or <math>\cos(2x - 59^\circ) = 0</math></p>	<p><b>M1</b> <b>DM1</b></p> <p><b>A1,A1</b></p> <p><b>M1</b></p>	<p><b>In each case the last A mark is for a second correct solution and no extra solutions within the range</b></p> <p><b>M1</b> for use of tan  <b>DM1</b> for dealing with <math>2x</math> correctly</p> <p><b>A1</b> for each</p> <p><b>M1</b> for either, then mark as above</p>
<p>(b)</p>	$2\cot^2 y + 3\operatorname{cosec} y = 0$ $2(\operatorname{cosec}^2 y - 1) + 3\operatorname{cosec} y = 0$ $2\operatorname{cosec}^2 y + 3\operatorname{cosec} y - 2 = 0$ $(2\operatorname{cosec} y - 1)(\operatorname{cosec} y + 2) = 0$ <p>One valid solution</p> $\operatorname{cosec} y = -2, \sin y = -\frac{1}{2}$ $y = 210^\circ, 330^\circ$ <p><b>Alternative:</b></p> $2\frac{\cos^2 y}{\sin^2 y} + \frac{3}{\sin y} = 0$ <p>leads to <math>2\sin^2 y - 3\sin y - 2 = 0</math></p> <p>and <math>\sin y = -\frac{1}{2}</math> only</p> $y = 210^\circ, 330^\circ$	<p><b>M1</b></p> <p><b>M1</b></p> <p><b>A1,A1</b></p> <p><b>M1</b></p> <p><b>M1</b></p> <p><b>A1A1</b></p>	<p><b>M1</b> for use of correct identity</p> <p><b>M1</b> for attempt to factorise a 3 term quadratic equation</p> <p><b>A1</b> for each</p> <p><b>M1</b> for use of <math>\cot y = \frac{\cos y}{\sin y}</math> and  <math>\operatorname{cosec} y = \frac{1}{\sin y}</math></p> <p><b>M1</b> for attempt to factorise a 3 term quadratic equation</p>
<p>(c)</p>	$3\cos(z + 1.2) = 2$ $\cos(z + 1.2) = \frac{2}{3}$ $(z + 1.2) = 0.8411, 5.442, 7.124$ $z = 4.24, 5.92$	<p><b>M1</b></p> <p><b>A1</b> <b>A1A1</b></p>	<p><b>M1</b> for correct order of operations to end up with 0.8411 radians or better  <b>A1</b> for one of 5.441 or 7.124 (or better)  <b>A1</b> for each valid solution</p>